According to DIN 740 part 2

# **BELLOWS COUPLINGS**





#### **SYMBOLS**

 $T_{KN}$  = Rated torque of the coupling (Nm)

T<sub>AS</sub> = Peak torque of the drive system e.g. max. acceleration torque of drive (Nm) or max. braking torque of load (Nm)

J<sub>L</sub> = Total load inertia (e.g. spindle + slide + workpiece + 1/2 of coupling) (kgm²)

J<sub>A</sub> = Total driving inertia (motor [including gear ratio] + 1/2 of coupling) (kgm<sup>2</sup>)

 $C_{T}$  = Torsional stiffness of the coupling (Nm/rad)

 $f_{\rm e}$  = Natural frequency of the two mass system (Hz)

 $f_{er}$  = Excitation frequency of the drive (Hz)

 $\phi$  = Torsional deflection (degree)

Shock or Load Factor S <sub>A</sub>									
uniform load	non-uniform load	highly dynamic load							
1	2	3-4							
Common factor for servo drives in machine tools: $S_A = 2-3$									

### ACCORDING TO TORQUE

Couplings are normally sized for the highest torque to be regularly transmitted. The peak torque of the application should not exceed the rated torque of the coupling. The following calculation provides an approximation of the minimum required coupling size, and allows for the maximum rated speed and misalignment to exist in the application:

$$T_{KN} \ge 1.5 \cdot T_{AS}$$
 (Nm)

### ACCORDING TO ACCELERATION TORQUE

A more detailed calculation takes acceleration and the driving and driven moments of inertia into account. A strong inertia ratio diminishes the effect of the load factor in the sizing calculation.

$$T_{KN} \geqq T_{AS} \cdot S_{A} \cdot \frac{J_{L}}{J_{A} + J_{L}} \text{ (Nm)}$$

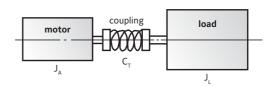
### ACCORDING TO RESONANT FREQUENCY

The torsional natural frequency of the coupling must be significantly higher or lower than that of the equipment. For the mechanical substitution model the two mass system applies.

In practice the following applies:  $f_e \ge 2 \cdot f_{er}$ 

$$f_{e} = \frac{1}{2 \cdot \pi} - \sqrt{C_{T} \cdot - \frac{J_{A} + J_{L}}{J_{A} \cdot J_{L}}} \quad (Hz)$$

Two Mass System



#### ACCORDING TO TORSIONAL DEFLECTION

To calculate transmission error as a result of torsional stress:

$$\varphi = \frac{180}{\pi} \cdot \frac{T_{AS}}{C_{T}}$$
 (degree)

# **ELASTOMER COUPLINGS**

EK

TX

ES

#### **SYMBOLS**

 $T_{\kappa_N}$  = Rated torque of the coupling (Nm)

 $T_{Kmax}$  = Maximum torque rating of the coupling (Nm)

T<sub>s</sub> = Peak torque applied to the coupling (Nm)

 $T_{AS}$  = Peak torque of the drive system (Nm)

 $T_{AN}$  = Nominal torque of the drive system (Nm)

 $T_{LN}$  = Nominal torque of the load (Nm)

P = Drive power (kW)

n = Rotational speed (min.-1)

 $J_A$  = Total driving inertia

(motor [including gear ratio] + 1/2 of coupling) (kgm²)

 $J_L$  = Total load inertia

(e.g. spindle + slide + workpiece + 1/2 of coupling) (kgm²)

J<sub>1</sub> = Moment of inertia of driving coupling half (kgm²)

J<sub>2</sub> = Moment of inertia of driven coupling half (kgm²)

m = ratio of the moment of inertia of the drive to the load

v = Temperature at the coupling (observed radiant heat)

S = Temperature factor

 $S_A = Load factor$ 

 $S_7$  = Start factor (factor for the number of starts per hour)

 $Z_h$  = Number of starts per hour (1/h)

Temperature factor S <sub>v</sub>	A	В	С	E
Temperature (υ)	Sh 98 A	Sh 64 D	Sh 80 A	Sh 64 D
> -30°C to -10°C	1.5	1.3	1.4	1.2
> -10°C to +30°C	1.0	1.0	1.0	1.0
> +30°C to +40°C	1.2	1.1	1.3	1.0
> +40°C to +60°C	1.4	1.3	1.5	1.2
> +60°C to +80°C	1.7	1.5	1.8	1.3
> +80°C to +100°C	2.0	1.8	2.1	1.6
> +100°C to +120°C	-	2.4	-	2.0
> +120°C to +150°C	_	_	_	2.8

Start factor S <sub>z</sub>			
Z <sub>h</sub>	up to 120	120 to 240	over 240
S,	1.0	1.3	contact us

Shock or Load Factor S <sub>A</sub>									
uniform load	non-uniform load	highly dynamic load							
1	1.8	2.5							

### COUPLING SELECTION FOR OPERATION WITHOUT SHOCK OR REVERSAL

The rated torque of coupling  $(T_{KN})$  must be greater than the rated torque of the load  $(T_{LN})$ , taking into account the temperature at the coupling (Temperature factor  $S\upsilon$ ). Should  $T_{LN}$  be unknown,  $T_{AN}$  can be used as a substitute in the

#### Calculation

$${\sf T_{KN}} > {\sf T_{AN}} \cdot {\sf S_{v}}$$

Supplemental Calculation

$$T_{AN} = \frac{9,550 \cdot P}{n}$$

Sample calculation: (without shock loads)

**Coupling conditions** 

 $v = 70^{\circ} \text{ C}$   $S_v = 1.7 \text{ (or } 70^{\circ}\text{/ Elastomer Type A)}$ 

Drive for centrifugal pump

$$T_{\Delta N} = 85 \text{ Nm}$$

Calculation:  $T_{KN} > T_{AN} \times S_v$ 

 $T_{KN} > 85 \text{ Nm} \cdot 1,7$ 

T<sub>KN</sub> > <u>144.5 Nm</u> —

Result: Coupling model EK2/150/A (T<sub>KN</sub> = 160 Nm) is selected.

### COUPLING SELECTION FOR OPERATION WITH SHOCK LOADS

Same basic conditions as above. In addition, the maximum torque rating of the coupling  $(T_{Kmax})$  is dictated by peak torque (T<sub>s</sub>) due to shock loads.

Calculation

$$T_{_{KN}} > T_{_{AN}} \cdot S_{_{\scriptscriptstyle U}}$$

Calculation

$$\rm T_{Kmax} > \rm T_S \, \cdot \, S_Z \, \cdot \, S_\upsilon$$

Supplemental Calculation

$$T_{AN} = \frac{9,550 \cdot P_{LN}}{n}$$

Supplemental Calculation

$$T_{S} = \frac{T_{AS} \cdot S_{A}}{m+1}$$

$$m = \frac{J_A \cdot J_1}{J_1 \cdot J_2}$$

# SAFETY COUPLINGS

SK

SL

ES

#### **SYMBOLS**

 $T_{KN}$  = Rated torque of the coupling (Nm)

 $T_{AN}$  = Load torque (Nm)

 $T_{AS}$  = Peak torque of the motor (Nm)

 $J_L$  = Moment of inertia of the load (kgm<sup>2</sup>)

J<sub>A</sub> = Moment of inertia of the drive (kgm<sup>2</sup>)

 $P_{AN}$  = Drive power (kW)

 $\alpha$  = Angular acceleration —

t = Acceleration / deceleration time (s)

 $\omega$  = Angular velocity (1/s)

n = Drive speed (min -1)

s = Screw lead (mm)

 $F_{v}$  = Feed force (N)

η = Spindle efficiency

d<sub>o</sub> = pinion dia. (pulley) (mm)

 $C_{\tau}$  = Torsional stiffness of the coupling (Nm/rad)

 $J_{Masch.}$  = Total load inertia (e.g. spindle + slide + workpiece

+ 1/2 of coupling) (kgm<sup>2</sup>)

J<sub>Mot.</sub> = Total driving inertia (motor [including gear ratio]

+ 1/2 of coupling) (kgm<sup>2</sup>)

f<sub>e</sub> = Natural frequency of the two mass system (Hz)

 $\varphi$  = Torsional deflection (degree)

Shock or Load Factor S <sub>A</sub>								
uniform load	non-uniform load	highly dynamic load						
1 2 3								
Common factor for servo drives in machine tools: S <sub>A</sub> = 2-3								

#### ACCORDING TO DISENGAGEMENT TORQUE

Torque limiters are generally selected according to the required disengagement torque, which must be greater than the torque required for regular operation. The disengagement of the torque limiter is most commonly determined in accordance with the drive data. For this purpose, the following calculation applies:

$$T_{KN} \ge 1.5 \cdot T_{AS} (Nm)$$

or

$$T_{KN} \ge 9,550 \cdot \frac{P_{AN}}{n} \cdot 1.5 \text{ (Nm)}$$

ACCORDING TO ACCELERATION (START-UP WITH NO LOAD)

$$T_{KN} \ge \alpha \cdot J_{L} \ge \frac{J_{L}}{J_{A} + J_{L}} \cdot T_{AS} \cdot S_{A} (Nm)$$

$$\alpha = \frac{\omega}{n} = \frac{\pi \cdot n}{t \cdot 30}$$

ACCORDING TO ACCELERATION WITH LOAD (START-UP UNDER LOAD)

$$T_{KN} \ge \alpha \cdot J_{L} + T_{AN} \ge \left[ \frac{J_{L}}{J_{A} + J_{L}} \cdot (T_{AS} - T_{AN}) + T_{AN} \right] \cdot S_{A} (Nm)$$

ACCORDING TO LINEAR FEED FORCE

Spindle Drive (ball screw / lead screw)

$$T_{AN} = \frac{s \cdot F_{v}}{2,000 \cdot \pi \cdot \eta} \quad (Nm)$$

Belt Drive / Chain Drive

$$T_{AN} = \frac{d_0 \cdot F_v}{2,000} \quad (Nm)$$

ACCORDING TO RESONANT FREQUENCY (SK2 / SK3 / SK5 WITH METAL BELLOWS - ES2 / ESL WITH ELASTOMER RING)

The torsional natural frequency of the coupling must be significantly higher or lower than that of the equipment. For the mechanical substitution model the two mass system applies:

$$f_{e} = \frac{1}{2 \cdot \pi} - \sqrt{C_{T} \times \frac{J_{Masch} + J_{Mot}}{J_{Masch} \cdot J_{Mot}}}$$
 (Hz)

ACCORDING TO TORSIONAL DEFLECTION (SK2 / SK3 / SK5 WITH METAL BELLOWS - ES2 / ESL WITH ELASTOMER RING)

To calculate transmission error as a result of torsional stress:

$$\varphi = \frac{180}{\pi} \cdot \frac{\mathsf{T}_{AN}}{\mathsf{C}_{\mathsf{T}}} \quad (\mathsf{degree})$$

#### ACCORDING TO LOAD HOLDING FUNCTION SYSTEM

#### ► Load Holding Version

The SK1, SKP, and SKN models in the load holding version can secure a minimum of 2x their torque setting after disengagement. The SK2, SK3, and SK5 models can secure

only up to the torque rating of the flexible bellows after disengagement.

# LINE SHAFTS

ZA

ΕZ

#### **SYMBOLS**

A = Total length (mm)

AB = Distance between flextures (mm)

AB = (A - 2xN)

Z = Tube length (mm)

Z = (A - 2xH)

H = Length of coupling ends (mm)

N = Length to flexture (mm)

 $T_{AS}$  = Peak torque of the drive (Nm)

 $\varphi$  = Torsional deflection (degree)

 $C_{T}^{B}$  = Torsional stiffness of both flexible elements (Nm/rad)

 $C_T^{ZWR}$  = Torsional stiffness per 1m of tubing (Nm/rad)

 $C_T^{ZA}$  = Total torsional stiffness (Nm/rad)

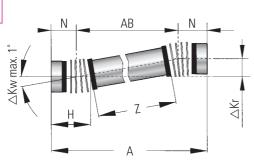
n<sub>k</sub> = Critical speed (1/min.)

 $C_{Tdyn}^{E}$  = Dynamic torsional stiffness of both

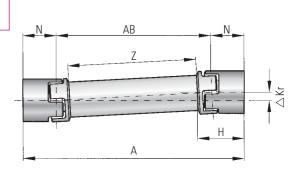
elastomer inserts (Nm/rad)

 $C_{Tdyn}^{EZ}$  = Total torsional stiffness (Nm/rad)





ΕZ



### **MODEL ZA**

Size	Torsional stiffness of both bellows bodies	Torsional stiffness per 1m of standard tubing	er 1m of standard 1m of CFK tubing coupling end		Length of coupling ends ZAE	Length to flexture	Maximum Axial misalignment
	C <sub>T</sub> <sup>B</sup> (Nm/rad)	C <sub>T</sub> <sup>ZWR</sup> (Nm/rad)	C <sub>T</sub> <sup>ZWR</sup> (Nm/rad)	H (mm)	H (mm)	N (mm)	Δ Ka (mm)
10	4,525	1,530	3,690	44.5	39.5	25	2
30	19,500	6,632	13,390	57.5	52	34	2
60	38,000	11,810	23,850	71	64	41	3
150	87,500	20,230	50,050	78	72	47	4
200	95,500	65,340	-	86	-	52	4
300	250,500	222,700	151,510	94	83	56	4
500	255,000	292,800	204,250	110	96	66	5
800	475,000	392,800	267,620	101	89	64	6
1500	1,400,000	728,800	-	92	_	56	4
4000	4,850,000	1,171,000	-	102	-	61	4

Table 1

### **MODEL EZ**

Size	Torsional stiffness of both flexible elements				Torsional stiffness per 1m of tubing	Working length EZ	Length to flexture	Max. axial misalignment
	Elastomer insert A C <sub>T</sub> <sup>B</sup> (Nm/rad)	Elastomer insert B C <sub>T</sub> <sup>B</sup> (Nm/rad)	C <sub>T</sub> <sup>ZWR</sup> (Nm/rad)	H (mm)	N (mm)	Δ Ka (mm)		
10	270	825	321	34	26	2		
20	1,270	2,220	1,530	46	33	4		
60	3,970	5,950	6,632	63	49	4		
150	6,700	14,650	11,810	73	57	4		
300	11,850	20,200	20,230	86	67	4		
450	27,700	40,600	65,340	99	78	4		
800	41,300	90,000	392,800	125	94	4		
2500	87,500	108,000	1,000,000	142	108	5		
4500	168,500	371,500	2,500,000	181	137	5		
9500	590,000	670,000	5,000,000	229	171	6		

Table 2

# MAXIMUM TRANSMITTABLE TORQUE BY BORE DIAMETER (Nm)

Size	Ø 6	Ø 8	Ø 16	Ø 19	Ø 25	Ø 30	Ø 32	Ø 35	Ø 45	Ø 50	Ø 55	Ø 60	Ø 65	Ø 70	Ø 75	Ø 80	Ø 90	Ø 120	Ø 140
10	6	12	32																
20		30	40	50	65														
60			65	120	150	180	200												
150				180	240	270	300	330											
300				300	340	450	520	570	630										
450						630	720	770	900	1120	1180	1350							
800								1050	1125	1200	1300	1400	1450	1500	1550	1600			
2500								1900	2600	2900	3200	3500	3800	4000	4300	4600	5200		
4500									5300	5800	6300	7000	7600	8200	8800	9400	10600	14100	
9500										9200	10100	11100	11900	12800	13800	14800	16700	22000	25600

# TEMPERATURE FACTOR S

В Sh 64 D Sh 98 A Temperature (φ) -30° to -10° 1.7 -10° to +30° 1.0 +40° to +60° 1.4 1.3 > +80° to +100° 2.0 1.8 > +100° to +120° 2.4

### ACCORDING TO TORSIONAL STIFFNESS

**Condition:** Line shaft ZA, size 150  $T_{AS} = 150 \text{ Nm}$ 

Wanted: Total torsional stiffness  $C_{\tau}^{ZA}$ 

$$(C_T^{ZA}) = \frac{87,500 \text{ Nm/rad} \times (20,230 \text{ Nm/rad} / 1.344 \text{ m})}{87,500 \text{ Nm/rad} + (20,230 \text{ Nm/rad} / 1.344 \text{ m})} = 12,842.8 \text{ [Nm/rad]}$$

$$(C_{T}^{ZA}) = \frac{C_{T}^{B} \cdot (C_{T}^{ZWR}/Z)}{C_{T}^{B} + (C_{T}^{ZWR}/Z)}$$
 (Nm/rad)

### ACCORDING TO TORSIONAL DEFLECTION

**Condition:** Line shaft ZA, size 150  $T_{AS} = 150 \text{ Nm}$  Wanted: Torsional deflection at maximum acceleration

torque  $T_{\rm AS}$ 

Measurement (A) of Line Shaft - 1.5m Length (Z) of Tubing = A-(2xH) = 1.344m

$$\varphi = \frac{180 \times 150 \text{ Nm}}{\pi \times 12,842.8 \text{ Nm/rad}} = 0.669^{\circ}$$

With a maximum torque of 150Nm the torsional deflection is  $0.669^{\circ}$ 

$$\varphi = \frac{180 \cdot T_{AS}}{\pi \cdot C_{T}^{ZA}} \text{ (degree)}$$

# LINE SHAFTS

ZA

ΕZ

#### ACCORDING TO MAXIMUM MISALIGNMENT



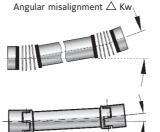


Lateral misalignment  $\triangle$  Kr





$$\Delta \text{ Kr}_{\text{max}} = \tan \Delta \frac{\text{Kw}}{2} \cdot \text{AB}$$
  
 $\Delta \text{AB} = A - 2xN$ 





Axial misalignment  $\triangle$  Ka





See table 1+2 Pages 16+17

### R+W CALCULATION PROGRAM

Using proprietary software, R+W will calculate the specific mechanical details of exactly the model you plan to use. Overall length, tube materials (e.g. steel, aluminum, CFK), and other factors are used to determine a number of performance values unique to your line shaft coupling.

Critical speed

Torsional stiffness of tubing

Overall stiffness
Torsional deflection

Total Weight

Moment of inertia

Maximum misalignment

 $n_k = 1/\min$ 

 $C_T^{ZWR} = Nm/rad$  $C_T^{ZA} = Nm/rad$ 

 $\varphi$  = degree-min-sec

m = kg

 $J = kgm^2$   $\triangle Kr = mm$ 

# DISC PACK COUPLINGS

LP

### **SYMBOLS**

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 (Nm)

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 (Nm)

